

# CICLO DE RANKINE IDEAL

## EXERCÍCIO



Fonte de Calor



$Q_g$

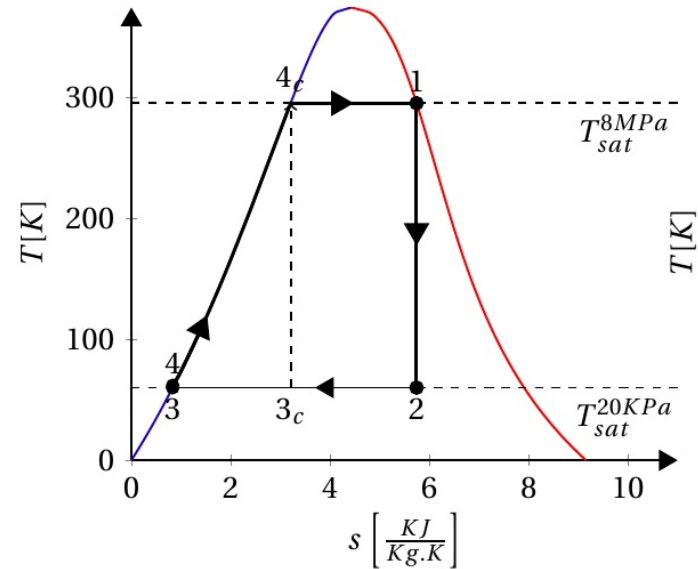
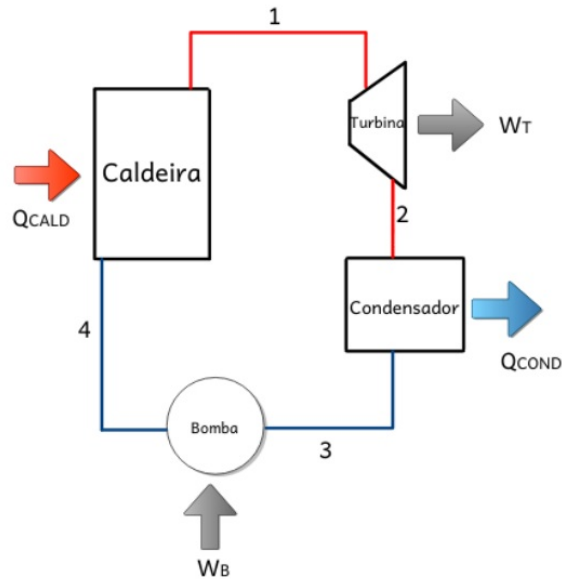


$Q_f$



Fonte Fria

(Ambiente ou Sumidouro)

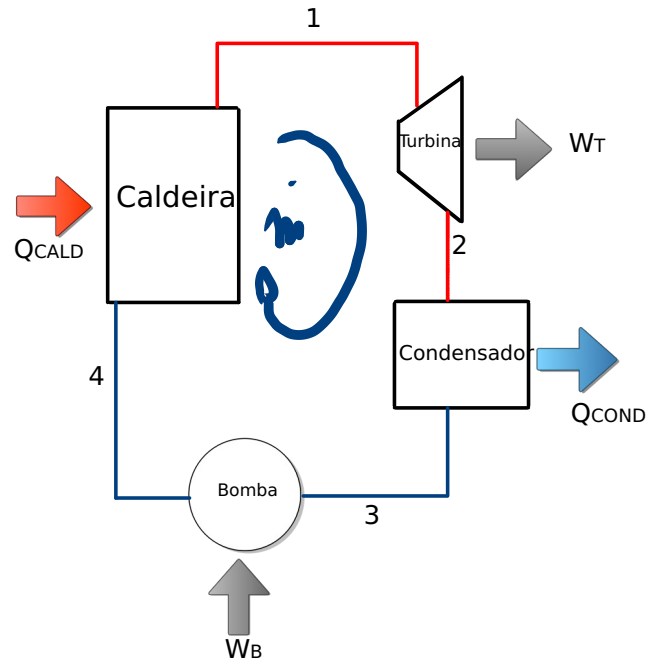


## Ciclo de geração de Potência a Vapor de Rankine

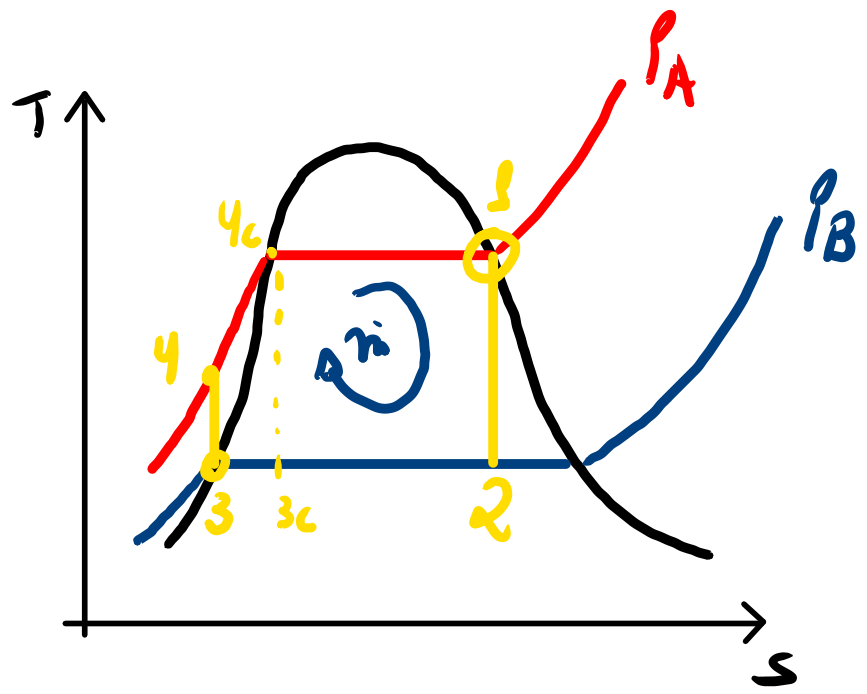
Água é o fluido de trabalho em um ciclo de potência a vapor de Rankine ideal. Vapor saturado entra na turbina a 8 [MPa] e líquido saturado entra na bomba a 20 [KPa]. Determine:

- a) Trabalho desenvolvido pela turbina e bomba
- b) Transferência de calor na caldeira e no condensador
- c) bwr
- d) Eficiência térmica
- e) Eficiência de Carnot

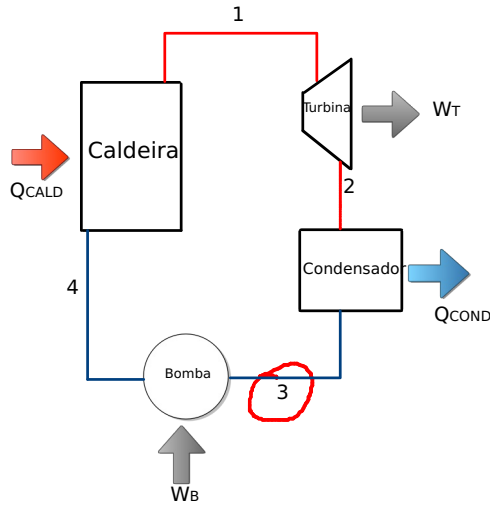
1. Desenhe os componentes do ciclo e identifique-os



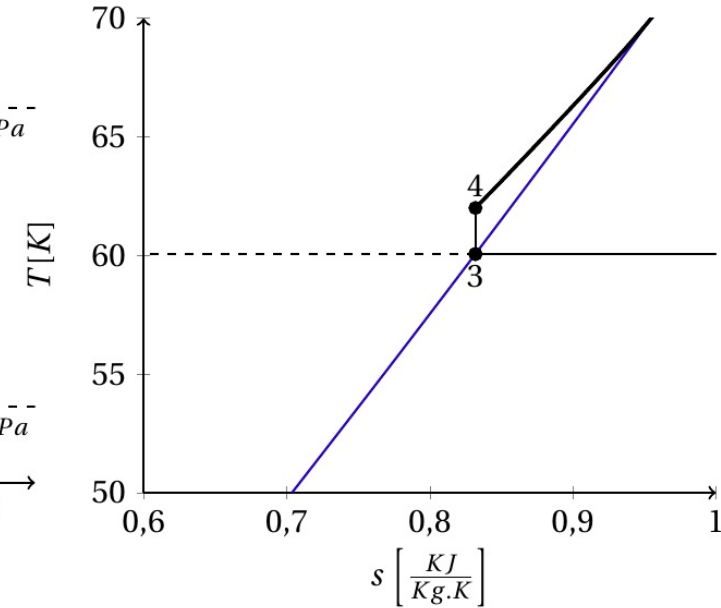
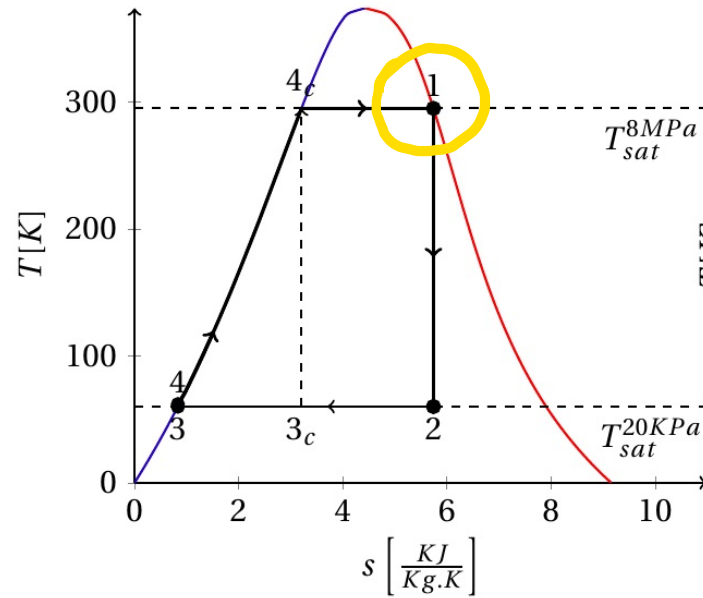
2. Desenhe o diagrama T-s



1. Desenhe os componentes do ciclo e identifique-os



2. Desenhe o diagrama T-s

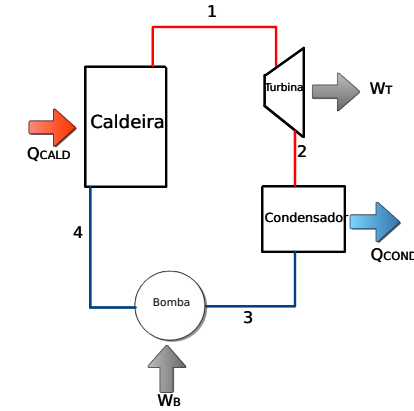


3. Faça uma tabela dos estados

Estado	P[KPa]	T[°C]	x	v[m <sup>3</sup> /Kg]	h[KJ/Kg]	s[KJ/Kg.K]
1	8000	T <sub>s</sub> (P <sub>1</sub> )	↓	~	h <sub>v</sub>	s <sub>v</sub>
2	20	T <sub>s</sub> (P <sub>2</sub> )		~		= s <sub>1</sub>
3	20	T <sub>s</sub> (P <sub>3</sub> )	0	v <sub>3</sub>	h <sub>L</sub>	s <sub>L</sub>
4	8000	?		~		= s <sub>3</sub>

4. Preencha os valores conhecidos na tabela

Estado	P[KPa]	T[°C]	x	v[m <sup>3</sup> /Kg]	h[KJ/Kg]	s[KJ/Kg.K]
1	8000	T <sub>s1</sub>	1	v <sub>1</sub> = v <sub>v</sub>	h <sub>1</sub> = h <sub>v</sub>	s <sub>1</sub> = s <sub>v</sub>
2	20					s <sub>2</sub> = s <sub>1</sub>
3	20	T <sub>s3</sub>	0	v <sub>3</sub> = v <sub>L</sub>	h <sub>3</sub> = h <sub>L</sub>	s <sub>3</sub> = s <sub>L</sub>
4	8000					s <sub>4</sub> = s <sub>3</sub>

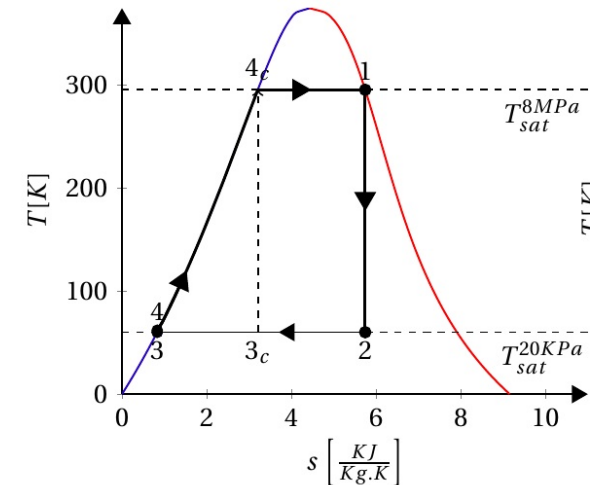


5. Calcule as propriedades restantes

P	T	v <sub>L</sub>	v <sub>v</sub>	u <sub>L</sub>	u <sub>LV</sub>	u <sub>v</sub>	h <sub>L</sub>	h <sub>LV</sub>	h <sub>v</sub>	s <sub>L</sub>	s <sub>LV</sub>	s <sub>v</sub>
7000	285,88	0,001351	0,02737	1257,51	1322,97	2580,48	1266,97	1505,10	2772,07	3,1210	2,6922	5,8132
8000	295,06	0,001384	0,02352	1305,54	1264,25	2569,79	1316,61	1441,33	2757,94	3,2067	2,5365	5,7431
9000	303,40	0,001418	0,02048	1350,47	1207,28	2557,75	1363,23	1378,88	2742,11	3,2857	2,3915	5,6771

3. Faça uma tabela dos estados

Estado	P[KPa]	T[°C]	x	v[m <sup>3</sup> /Kg]	h[KJ/Kg]	s[KJ/Kg.K]
1	8000	295,06	1	~	2757,94	5,7431
2	20			~		5,7431
3	20		0			
4	8000			~		



3. Faça uma tabela dos estados

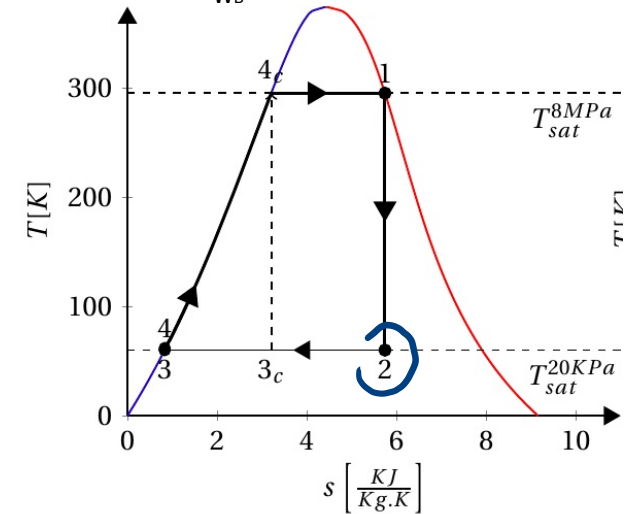
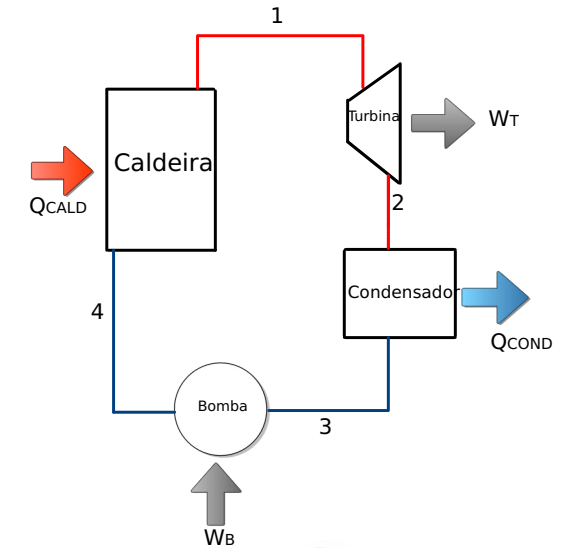
Estado	P[KPa]	T[°C]	x	v[m <sup>3</sup> /Kg]	h[KJ/Kg]	s[KJ/Kg.K]
1	8000	235,06	1	~	2757,94	5,7431
2	20	60,06		~		5,7431
3	20	60,06	0	v <sub>L</sub>	h <sub>L</sub>	s <sub>L</sub>
4	8000			~		

P	T	v <sub>L</sub>	v <sub>v</sub>	u <sub>L</sub>	u <sub>v</sub>	h <sub>L</sub>	h <sub>v</sub>	s <sub>L</sub>	s <sub>v</sub>
15	53,97	0,001014	10,02218	225,90	2222,83	2448,73	225,91	0,7548	7,2526
20	60,06	0,001017	7,64937	251,35	2205,36	2456,71	251,38	0,8319	7,9085
25	64,97	0,001020	6,20424	271,88	2191,21	2463,08	271,90	0,8930	8,3383

P[KPa]	T[°C]	h <sub>L</sub> [KJ/Kg]	h <sub>v</sub> [KJ/Kg]	s <sub>L</sub> [KJ/Kg.K]	s <sub>v</sub> [KJ/Kg.K]
20	60,06	251,38	2609,70	0,8319	7,9085

$$x_2 = \frac{5,7431 - 0,8319}{7,0766} = 0,694$$

$$h_1 = 251,38 + 0,694(2358,33) = 1888,074$$

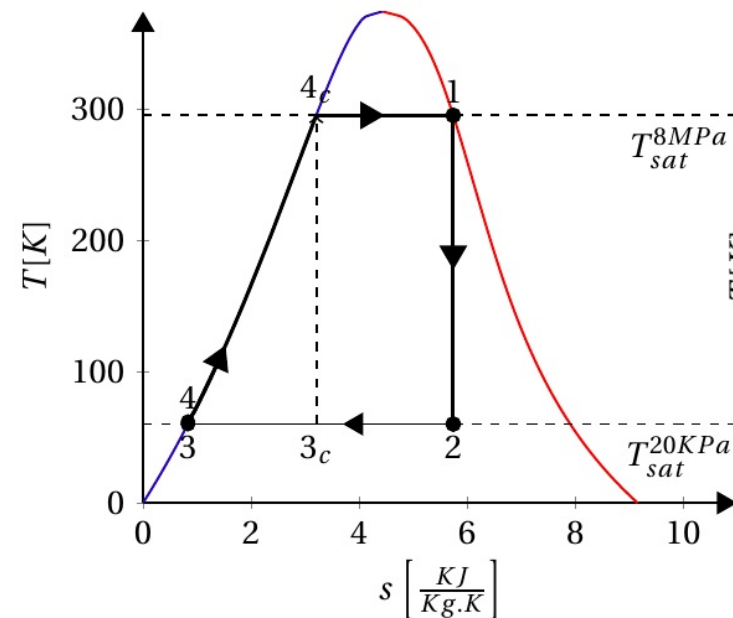
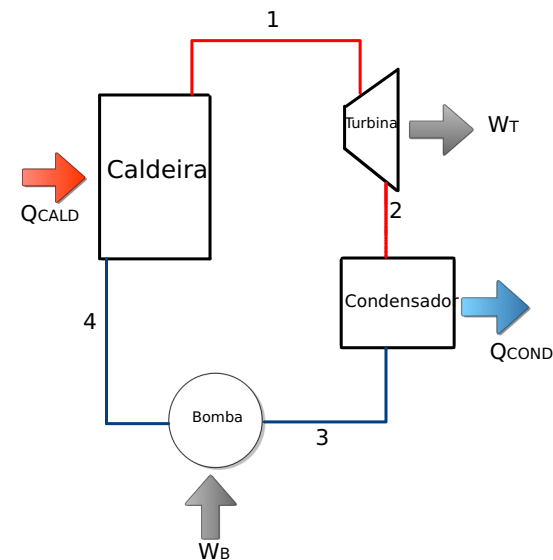


3. Faça uma tabela dos estados

Estado	P[KPa]	T[°C]	x	v[m <sup>3</sup> /Kg]	h[KJ/Kg]	s[KJ/Kg.K]
1	8000	295,06	1	~	2757,94	5,7431
2	20	60,06	x <sub>2</sub>	~	1888,074	5,7431
3	20		0	0,001017	251,38	0,8319
4	8000			~		0,8319

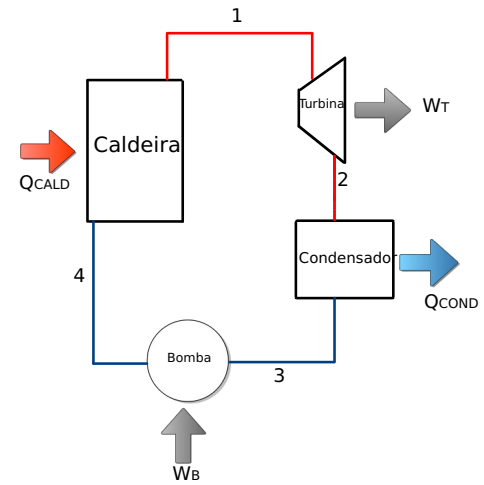
15	53,97	0,001017	10,02218	225,90	2222,83	2448,73	225,91	2373,14	2599,06	0,7548	7,2536	8,0084
20	60,06	0,001017	7,64937	251,35	2205,36	2456,71	251,38	2358,33	2609,70	0,8319	7,0766	7,9085
25	64,97	0,001017	6,20424	271,88	2191,21	2463,08	271,90	2346,29	2618,19	0,8930	6,9383	7,8313

P[KPa]	T[°C]	h <sub>L</sub> [KJ/Kg]	h <sub>v</sub> [KJ/Kg]	s <sub>L</sub> [KJ/Kg.K]	s <sub>v</sub> [KJ/Kg.K]
20	60,06	251,38	2609,70	0,8319	7,9085



3. Faça uma tabela dos estados

Estado	P[KPa]	T[°C]	x	v[m <sup>3</sup> /Kg]	h[KJ/Kg]	s[KJ/Kg.K]
1	8000	295,06	↓	~	2757,94	5,7431
2	20	60,06	x <sub>2</sub>	~	1888,074	5,7431
3	20	60,06	0	0,001017	251,38	0,8319
4	8000			~		0,8319

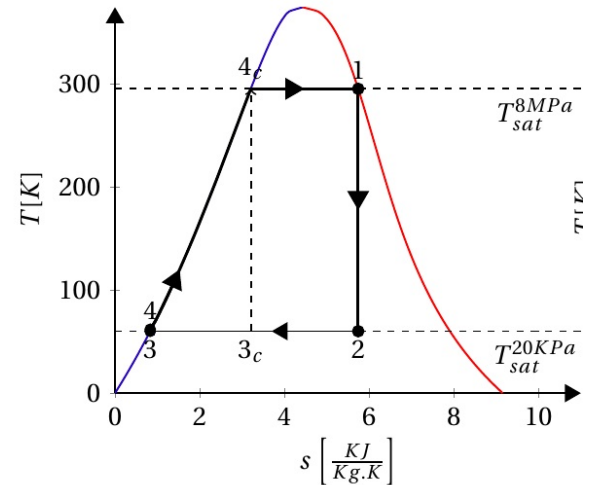


P[KPa]	T[°C]	h <sub>L</sub> [KJ/Kg]	h <sub>v</sub> [KJ/Kg]	s <sub>L</sub> [KJ/Kg.K]	s <sub>v</sub> [KJ/Kg.K]
8000	295,06	1316,61	2757,94	3,2067	5,7431

$$w_b = h_4 - h_3 \approx \vartheta_3 (P_4 - P_3)$$

$$h_4 - 251,38 = 0,001017 (8000 - 20)$$

$$h_4 = 259,49566 \frac{\text{kJ}}{\text{kg}}$$



## Ponto 4: temperatura

$$h_4 = 259,49566$$

Água saturada: tabela em função da pressão

Pressão kPa	Temp. °C	Volume específico (m <sup>3</sup> /kg)		Energia interna (kJ/kg)			Entalpia (kJ/kg)			Entropia (kJ/kg K)		
		Líquido sat.	Vapor sat.	Líquido sat.	Evap.	Vapor sat.	Líquido sat.	Evap.	Vapor sat.	Líquido sat.	Evap.	Vapor sat.
$P$	$T$	$v_l$	$v_v$	$u_l$	$u_{lv}$	$u_v$	$h_l$	$h_{lv}$	$h_v$	$s_l$	$s_{lv}$	$s_v$
0,6113	0,01	0,001000	206,132	0	2375,3	2375,3	0,00	2501,30	2501,30	0,0000	9,1562	9,1562
1	6,98	0,001000	129,20802	29,29	2355,69	2384,98	29,29	2484,89	2514,18	0,1059	8,8697	8,9756
1,5	13,03	0,001001	87,98013	54,70	2338,63	2393,32	54,70	2470,59	2525,30	0,1956	8,6322	8,8278
2	17,50	0,001001	67,00385	73,47	2326,02	2399,48	73,47	2460,02	2533,49	0,2607	8,4629	8,7236
2,5	21,08	0,001002	54,25385	88,47	2315,93	2404,40	88,47	2451,56	2540,03	0,3120	8,3311	8,6431
3	24,08	0,001003	45,66502	101,03	2307,48	2408,51	101,03	2444,47	2545,50	0,3545	8,2231	8,5775
4	28,96	0,001004	34,80015	121,44	2293,73	2415,17	121,44	2432,93	2554,37	0,4226	8,0520	8,4746
5	32,88	0,001005	28,19251	137,79	2282,70	2420,49	137,79	2423,66	2561,45	0,4763	7,9187	8,3950
7,5	40,29	0,001008	19,23775	168,76	2261,74	2430,50	168,77	2406,02	2574,79	0,5763	7,6751	8,2514
10	45,81	0,001010	14,67355	191,79	2246,10	2437,89	191,81	2392,82	2584,63	0,6492	7,5010	8,1501
15	53,97	0,001014	10,02218	225,90	2222,83	2448,73	225,91	2373,14	2599,06	0,7548	7,2536	8,0084
20	60,06	0,001017	7,64937	251,35	2205,36	2456,71	251,38	2358,33	2609,70	0,8319	7,0766	7,9085
25	64,97	0,001020	6,20424	271,88	2191,21	2463,08	271,90	2346,29	2618,19	0,8930	6,9383	7,8313
30	69,10	0,001022	5,22918	289,18	2179,22	2468,40	289,21	2336,07	2625,28	0,9439	6,8247	7,7686
40	75,87	0,001026	3,99345	317,51	2159,49	2477,00	317,55	2319,19	2636,74	1,0258	6,6441	7,6700

T	$h_L$
60,06	251,38
$T_4$	259,49566
64,97	271,9

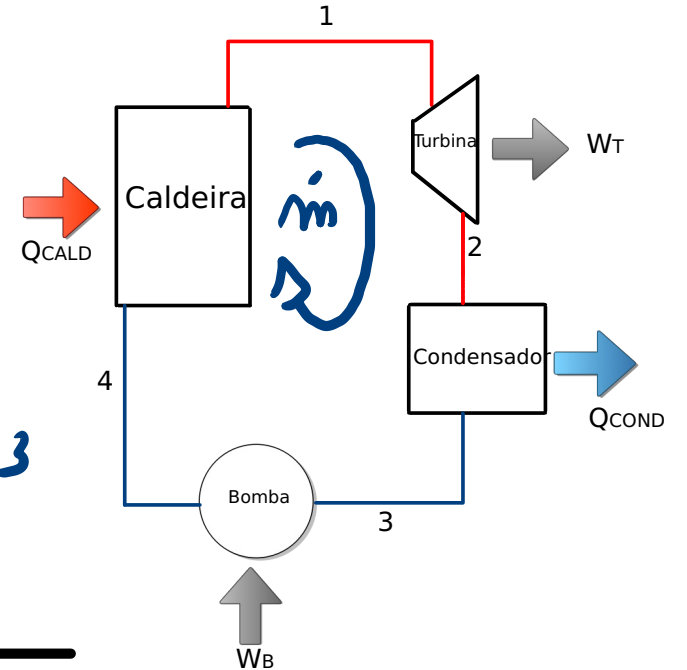
Logo:  $T_4 = 62,00 [C]$

60,06 °C

Estado	P[KPa]	T[°C]	x	v[m <sup>3</sup> /Kg]	h[KJ/Kg]	s[KJ/Kg.K]
1	8000	295,06	1	0,2352	2757,94	5,7431
2	20	60,06		0,694	1888,067	5,7431
3	20	60,06	0	0,001017	251,38	0,8319
4	8000	62		0,001017	259,49566	0,8319

$$de = \delta q + \delta w$$

Componente	q [KJ/Kg]	w [KJ/Kg]
CALDEIRA	$h_1 - h_4 = 2498,4434$	0
TURBINA	0	$h_2 - h_1 = -863,873$
CONDENSADOR	$h_3 - h_2 = -1636,687$	0
Bomba	0	$+ 8,11566$
	<b>863,75</b>	<b>-863,75</b>



Componente	$q$ [kJ/kg]	$w$ [kJ/kg]
CALDEIRA	$h_1 - h_4 = 2498,4434$	0
TURBINA	0	$h_2 - h_1 = -869,873$
CONDENSADOR	$h_3 - h_2 = -1636,687$	0
Bomba	0	+ 8,11566
	<b>861,75</b>	<b>-861,75</b>

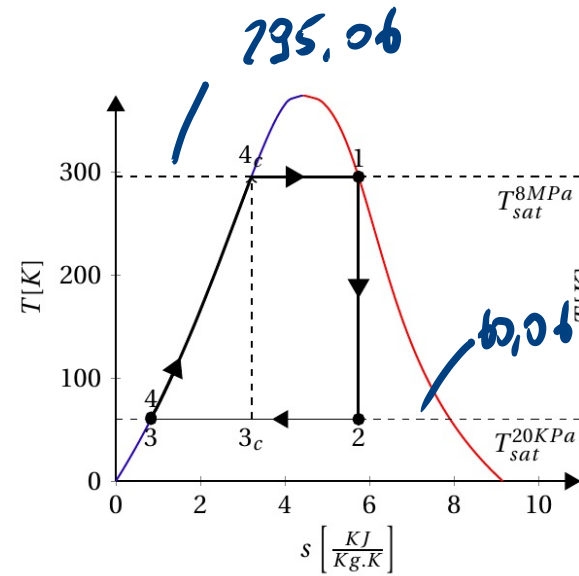
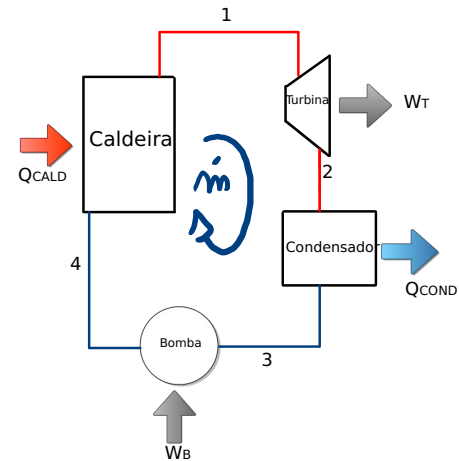
$$\eta = \frac{861,75}{2498,4434} = 0,3449$$

$$bwn = \frac{8,11566}{869,873} = 0,93\%$$

3448%

$$\eta_c = 1 - \frac{T_F}{T_g}$$

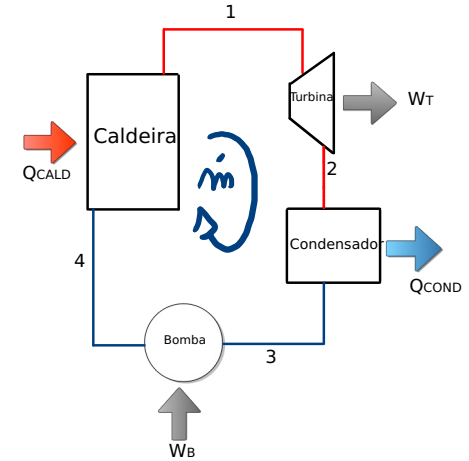
$$\eta_c = 41,35\%$$



# TEMPERATURA MÉDIA DA FONTE QUENTE :

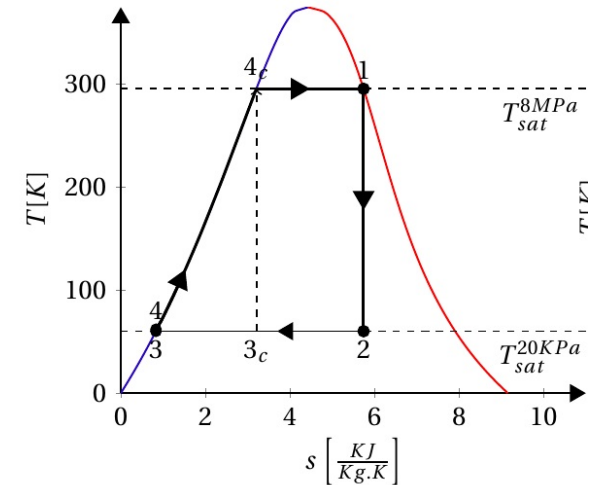
$$ds = \frac{\delta q}{T}$$

Estado	P[KPa]	T[°C]	x	v[m <sup>3</sup> /Kg]	h[KJ/Kg]	s[KJ/Kg.K]
1	8000	295,06	1	0,2352	2757,94	5,7431
2	20	60,06		0,694	1888,067	5,7431
3	20	60,06	0	0,001017	251,38	0,8319
4	8000	62		0,001017	259,49566	0,8319



$$T_g = \frac{q_g}{ds_g} = \frac{2498,4434 \text{ kJ/kg}}{5,7431 - 0,8319 \text{ kJ/kg.K}}$$

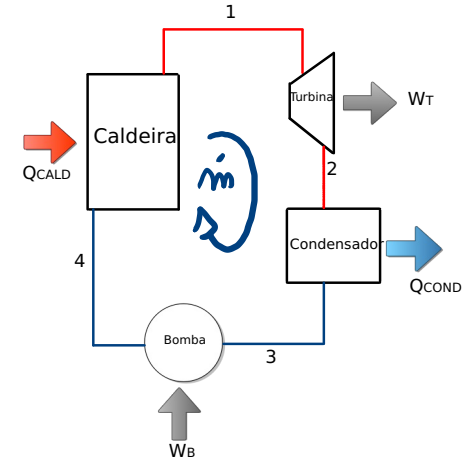
$$T_g = 508,7236 \text{ K} = 235,56^\circ\text{C} \quad (295,06)$$



# TEMPERATURA MÉDIA DA FONTE QUENTE :

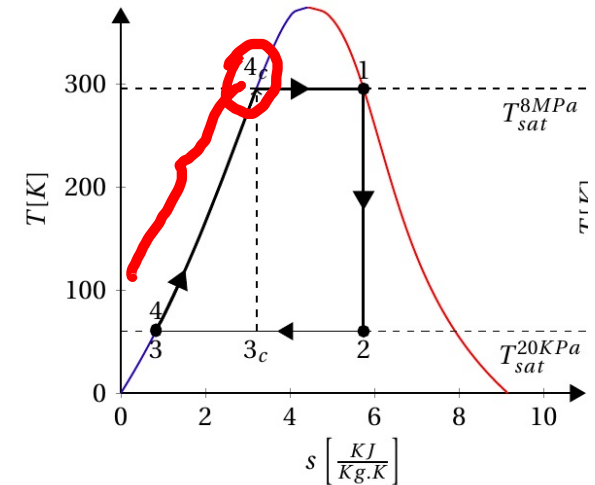
$$ds = \frac{\delta q}{T}$$

Estado	P[KPa]	T[°C]	x	v[m <sup>3</sup> /Kg]	h[KJ/Kg]	s[KJ/Kg.K]
1	8000	295,06	1	0,2352	2757,94	5,7431
2	20	60,06		0,694	1888,067	5,7431
3	20	60,06	0	0,001017	251,38	0,8319
4	8000	62		0,001017	259,49566	0,8319



$$T_g = \frac{q_g}{ds_g} = \frac{2498,4434 \text{ kJ/kg}}{5,7431 - 0,8319 \text{ kJ/kg.K}}$$

$$T_g = 508,7236 \text{ K} = 235,56^\circ\text{C} \quad (295,06)$$



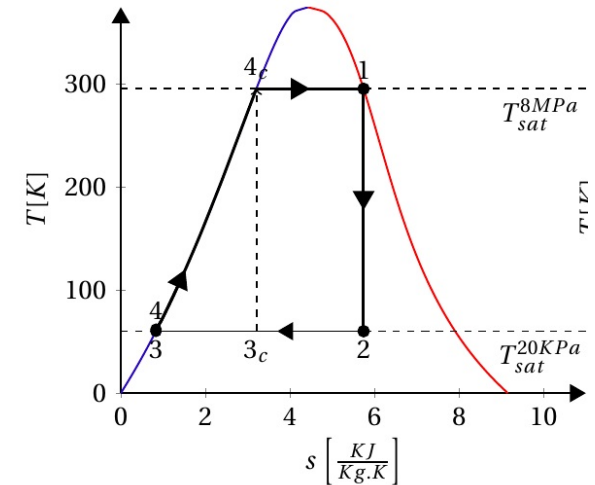
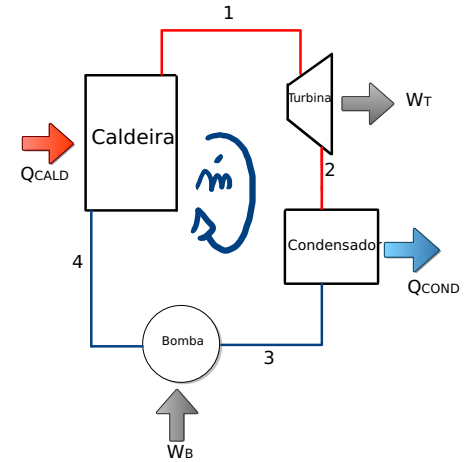
# TEMPERATURA MÉDIA DA FONTE FRIA

Estado	P[KPa]	T[°C]	x	v[m <sup>3</sup> /Kg]	h[KJ/Kg]	s[KJ/Kg.K]
1	8000	295,06	1	0,2352	2757,94	5,7431
2	20	60,06		0,694	1888,067	5,7431
3	20	60,06	0	0,001017	251,38	0,8319
4	8000	62		0,001017	259,49566	0,8319

$$T_F = \frac{Q_F}{ds_F} = \frac{-3636,687 \text{ kJ/Kg}}{0,8319 - 5,7431 \text{ kJ/Kg.K}}$$

$$T_F = 333,256 \text{ K} = 60,096 \text{ °C}$$

$$ds = \frac{\delta q}{T}$$

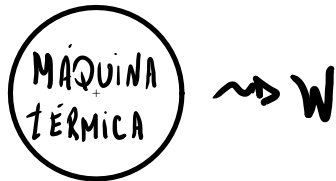


# Rendimento máximo DE RANKINE IDEAL

Fonte de Calor

$$T_a \quad 508,7236 \text{ K}$$

$Q_a$



$$T_f \quad 333,256 \text{ K}$$

Fonte Fria

(Ambiente ou Sumidouro)

$$\eta = 1 - \frac{333,256}{508,7236}$$

$$\eta = 0,3449$$



mesmo VALOR!!

The logo features a thick yellow circular border on a red background. Inside the circle, the text "CIÊNCIAS" and "TÉRMICAS" are stacked vertically in a bold, white, sans-serif font. Below them, ".com" is written in a smaller, white, sans-serif font.

**CIÊNCIAS**  
**TÉRMICAS**  
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